







Course Title: Measure Theory I

Course Code: MATH642

Program: Master Program in Mathematics

Department: Mathematics

College: Science

Institution: University of Tabuk, KSA

Version: 2

Last Revision Date: 1/12/1443 H







# Table of Contents:

Content	Page
A. General Information about the course	3
<ol> <li>Teaching mode (mark all that apply)</li> <li>Contact Hours (based on the academic semester)</li> </ol>	3
B. Course Learning Outcomes (CLOs), Teaching Strategies and Assessment Methods	4
C. Course Content	5
D. Student Assessment Activities	5
E. Learning Resources and Facilities	6
1. References and Learning Resources	6
2. Required Facilities and Equipment	6
F. Assessment of Course Quality	6
G. Specification Approval Data	7





A. General information about the course:					
Course	e Identificatior	n l			
1. Cre	edit hours:	3 H			
2. Cou	rse type				
a. Ui	niversity $\Box$	College $\Box$	Department 🛛	Track	Others 🗆
b. Re	equired 🗆	Elective⊠			
3. Lev	el/year at whic	ch this course is	s offered:		
Leve	I-2 or higher				
<ul> <li>4. Course general description</li> <li>Sigma-Algebras, Monotone Classes, Measure Basic Concepts, Outer Measure, Extension Theorems, Completion and Approximation Theorems, Lebesgue and Lebesgue-Stieltjes</li> <li>Measures, Distributions and Probability Measure, Measurable Functions, Integration with respect to a measure, Basic Theorems, Convergence of Measurable Functions.</li> <li>5. Pre-requirements for this course (if any): None</li> <li>6. Co-requirements for this course (if any): None</li> <li>7. Course Main Objective(s)</li> <li>Upon completion of the course students will be able to:</li> <li>a. Understand and apply basic concepts of measure and integration theory.</li> <li>b. Use abstract methods to solve problems.</li> <li>c. Use a wide range of references and critical thinking.</li> </ul>					
measur	re theory.	<i>,</i>			
<b>1.</b> Tea	aching mode	(Mark all that a	apply)		
No	Mode	of Instruction	Contact	Hours	Percentage
1.	E looming	assroom	43	)	100 %
Ζ.	Hybrid				
3.	• Tradit • E-lear	tional classroom			
4.	Distance learn	ning			
2. Contact Hours (based on the academic semester)					
No		A	Activity		Contact Hours
1.	Lectures				3 H /week
2.	Laboratory/Stu	idio			
3.	Field				
4.	Tutorial				

5. Others (specify)

Total

B. Course Learning Outcomes (CLOs), Teaching Strategies and Assessment Methods





Code	Course Learning Outcomes	Code of CLOs aligned with program	Teaching Strategies	Assessment Methods
1.0	Knowledge and understanding: Th	e students will	be able to:	
1.1	Recall the main concepts and theorems of measures and outer measures.	K1	Lectures, Group works, Presentations	Exams, Quizzes, Research
1.2	Prove in-depth knowledge of measurable functions and related theorems.	K2	Classroom discussion, Seminar, Case study, problem solving	project, presentation, interactive
1.3	Enhance finite cases from infinite	K3	session	participation,
	in medsure theory.			Survey
2.0	Skills: The students will be able to	:		
2.1	Solve and analyze problems using techniques and methods from measure theory.	S1	Lectures, Group works,	Exams, Quizzes, Research
2.2	Prove theorems and interpret results using measure theory.	S2	Presentations, Classroom discussion, Seminar. Case study.	project, presentation,
2.3	Clearly and apply measure theory to solve concrete problems.	S3	problem solving session	discussion and participation, Survey
2.4				·
3.0	Values, autonomy, and responsibi	lity: The studen	ts will be able to:	
3.1	Work in teams/groups with great consideration of ethics.	V1	Lectures, Group works, Presentations,	Research project, presentation.
3.2	Manage duties and time adequately.	V2	Classroom discussion, Seminar, Case study, problem solving session	interactive discussion and participation, Survey

## C. Course Content

No	List of Topics	Contact Hours
1	Measures: algebras, σ-algebras, positive measures,	3





2	Outer measures, Caratheodory's theorem.	3
3	Measures: extension of measures from algebras to $\sigma$ -algebras,	3
4	Lebesgue, and Lebesgue-Stieltjes Measures	3
5	Measurable functions: approximation by step functions, modes of convergence of sequences of functions, Egoroff's theorem.	3
6	Definition and example of Measurable functions	3
7	Measurable functions: Distributions and Probability Measure	3
7	Mid-Exam #	-
8	Integration: integration of nonnegative functions.	3
9	Integration: Lebesgue monotone convergence theorem.	3
10	Integration: Fatou's lemma,	3
11	Lebesgue dominated convergence theorem, comparison with Riemann's integral	3
12	Product measures: construction of product measures, monotone classes.	3
13	Product measures: Tonelli's and Fubini's theorem,	3
14	The Lebesgue integral on Rn	3
15	Product measures: convergence types of measurable functions	3
16+17	Review & Final Exam	
	Total	45

### **D. Students Assessment Activities**

No	Assessment Activities *	Assessment timing (in week no)	Percentage of Total Assessment Score
1.	Home works and Assignments	Weekly basis	20%
2.	Mid-term exam	6th week	25%
3.	Presentation and discussion	During the semester	15%
4.	Final exam	At the end of the semester	40 %

\*Assessment Activities (i.e., Written test, oral test, oral presentation, group project, essay, etc.)

### E. Learning Resources and Facilities

#### **1. References and learning resources**

Essential References	Ammar Khanfer , Measure Theory and Integration, Springer Nature Singapore (2022).
Supportive References	Measure Theory, By Vladimir I. Bogachev, Springer 2007.
Electronic Materials	Saudi electronic library.
Other Learning Materials	None

### 2. Required facilities and equipment

Items	Resources
facilities (Classrooms, laboratories, exhibition rooms, simulation rooms, etc.)	Lecture room with capacity of 15 students at most and equipped with White Board, Library





Items	Resources
Technology equipment (projector, smart board, software)	Overhead projector and internet connection.
Other equipment (depending on the nature of the specialty)	

## F. Assessment of Course Quality

Assessment Areas/Issues	Assessor	Assessment Methods
Effectiveness of teaching	Students	Direct and Indirect
Effectiveness of students' assessment	Teacher	Direct
Quality of learning resources	Students	Indirect
The extent to which CLOs have been achieved	Teacher, Quality Committee	Direct and Indirect
Other		

Assessor (Students, Faculty, Program Leaders, Peer Reviewer, Others (specify) Assessment Methods (Direct, Indirect)

## G. Specification Approval Data

Council / Committee	Approval by the Department Council
Reference No.	DEPARTMENT COUNCIL NO (26)
Date	11/9/1444 H

