



Course Specifications

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|----------------------|------------------------------------|
| Course Title: | Functional Analysis |
| Course Code: | Math 415 |
| Program: | Bachelor of Science in Mathematics |
| Department: | Mathematics |
| College: | Science |
| Institution: | University of Tabuk |

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A. Course Identification

| | |
|---|---|
| 1. Credit hours: | 03 Hours/Week |
| 2. Course type: | |
| a. | University <input type="checkbox"/> College <input type="checkbox"/> Department <input checked="" type="checkbox"/> Others <input type="checkbox"/> |
| b. | Required <input checked="" type="checkbox"/> Elective <input type="checkbox"/> |
| 3. Level/year at which this course is offered: | L8/Y4 |
| 4. Pre-requisites for this course(if any): | Math 311 |
| 5. Co-requisites for this course(if any): | None |

6. Mode of Instruction (mark all that apply)

| No | Mode of Instruction | Contact Hours | Percentage |
|----|------------------------------------|---------------|------------|
| 1 | Traditional classroom / Blackboard | 45 | 100 % |
| 2 | Blended | | |
| 3 | E-learning | | |
| 4 | Distance learning | | |
| 5 | Other | | |

7. Contact Hours (based on academic semester)

| No | Activity | Contact Hours |
|----|-------------------|---------------|
| 1 | Lecture | 45 |
| 2 | Laboratory/Studio | |
| 3 | Tutorial | |
| 4 | Others (specify) | |
| | Total | 45 |

B. Course Objectives and Learning Outcomes

| |
|---|
| <p>1. Course Description</p> <p>The aim of the course is to introduce students to the basic concepts and fundamental theorems of functional analysis, and learn how to apply these theorems to solve problems.</p> |
| <p>2. Course Main Objective</p> <ul style="list-style-type: none"> Students will be able to recall the basic concepts of functional analysis through the study of function spaces, functions, operators and functionals and real-valued functions on the function spaces such as metric, norm and inner-product. Students recognize different types of operators and their applications. |



3. Course Learning Outcomes

| CLOs | | Aligned PLOs |
|------|---|--------------|
| 1 | Knowledge and Understanding: | |
| 1.1 | Students will be able to recall the basic concepts and theorems of functional analysis. | K1 |
| 2 | Skills : | |
| 2.1 | Students will be able to apply theorems and results that they have learnt in this course to solve complex problems. | S3 |
| 2.2 | Students will be able to justify the analytical procedures to prove the right target theorems. | S1 |
| 2.3 | Students will be able to demonstrate proficiency in communicating functional analysis theorems and concepts. | S5 |
| 3 | Values: | |
| 3.1 | Students will be able to develop enhanced self-learning. | V1 |
| | Students will be able to work independently and in groups. | V2 |

C. Course Content

| No | List of Topics | Contact Hours |
|--------------|--|---------------|
| 1 | Linear subspace, Linear dependence and Linear combination | 3 Hrs |
| 2 | Dimension and Basis, Spanning, Direct sum decomposition for $V(F)$ | 3 Hrs |
| 3 | Cauchy Schwarz inequality- Minkowski inequality, Polarization identity | 3 Hrs |
| 4,5 | Orthogonal sets of vectors, Orthogonalization (Gram-Schmidt) | 6 Hrs |
| 6 | Mid-Exam#1 | |
| 6 | Holder inequality, general Minkowski inequality | 3 Hrs |
| 7,8 | Metric and Metric spaces, Some topological notion in metric spaces | 6 Hrs |
| 9 | Convergent and completeness, Cauchy sequence, Convergent sequence, Complete metric space | 3 Hrs |
| 10 | Continuity and uniform continuity on metric spaces, Fixed points and Contraction mappings. | 3 Hrs |
| 11 | Mid-Exam#2 | |
| 11 | Banach Contraction Principle, Orthogonal system, Fourier coefficient | 3 Hrs |
| 12 | Bounded operators, Continuous, Linear functional in Hilbert H-adjoint operator, Self-adjoint operator, Normal operator, Unitary operator, Isometric operators, Symmetric operators, Positive Operators | 3 Hrs |
| 13 | Projection operators. Closed operator, Graph of an operator | 3 Hrs |
| 14 | The formal differential operator $(i \frac{d}{dx})$ – Eigenvalues and Eigenvectors, Spectrum of self-adjoint operator | 3 Hrs |
| 15 | Review and Final Exam | 3 Hrs |
| Total | | 45 Hrs |

D. Teaching and Assessment

1. Alignment of Course Learning Outcomes with Teaching Strategies and Assessment Methods



| Code | Course Learning Outcomes | Teaching Strategies | Assessment Methods |
|------------|--|---|---|
| 1.0 | Knowledge and Understanding | | |
| 1.1 | Recall the basic concepts and theorems of functional analysis. | Introducing new ideas through case study Lectures Class Discussions | Quizzes I II Midterm Exams Final Exams homework assignments. |
| 2.0 | Skills | | |
| 2.1 | Apply theorems and results that they have learnt in this course to solve complex problems. | - Lectures Group work - Case Study - Brainstorming | - Quizzes -Assignments -Midterm exams - Final exam |
| 2.2 | Justify the analytical procedures to prove the right target theorems. | | |
| 2.3 | Demonstrate proficiency in communicating functional analysis theorems and concepts. | | |
| 3.0 | Values | | |
| 3.1 | Students will be able to develop enhanced self-learning. | Cooperative learning and Teamwork | - Quizzes -Assignments -Class participation |
| 3.2 | Students will be able to work independently and in groups. | | |

2. Assessment Tasks for Students

| # | Assessment Task* | Week Due | Percentage of Total Assessment Score |
|---|------------------|-----------|--------------------------------------|
| 1 | Mid Exam 1 | Sixth | 25% |
| 2 | Mid Exam 2 | Eleventh | 25% |
| 3 | Quiz 1 | Seventh | 3% |
| 4 | Quiz 2 | Twelfth | 3% |
| 5 | Home Assignments | | 4% |
| 6 | Final Exam | Fifteenth | 40% |

*Assessment task (i.e., written test, oral test, oral presentation, group project, essay, etc.)

E. Student Academic Counseling and Support

Arrangements for availability of faculty and teaching staff for individual student consultations and academic advice :

Six office hours per week in the lecturer schedule.

F. Learning Resources and Facilities

1. Learning Resources

| | |
|---------------------------|--|
| Required Textbooks | Erwin Kreyszig , Introductory Functional Analysis with Applications, John Wiley and Sons, New York, 1989 . |
|---------------------------|--|



| | |
|---------------------------------------|--|
| | Balmohan V. Limaye, Linear Functional Analysis for Scientists and Engineers, Springer Singapore (2016) |
| Essential References Materials | <ul style="list-style-type: none"> ● Lax. P., Functional Analysis, Wiley-Inter Science, 2002. ● Rudin W., Functional Analysis, McGraw-Hill Science, 1991. ● John B. Conway, A Course in Functional Analysis (Graduate Texts in Mathematics), Second Edition, Springer, 2007. ● Bryan P. Rynne and Martin A. Youngson, Linear Functional Analysis, Second Edition, Springer Verlag, London, 2008. |
| Electronic Materials | None |
| Other Learning Materials | None |

2. Facilities Required

| Item | Resources |
|--|---|
| Accommodation (Classrooms, laboratories, demonstration rooms/labs, etc.) | 1.Lecture Room with max capacity of 30 students and equipped with White Board, Overhead projector and internet connection. 2.Library |
| Technology Resources (AV, data show, Smart Board, software, etc.) | Projectors |
| Other Resources (Specify, e.g. if specific laboratory equipment is required, list requirements or attach a list) | None |

G. Course Quality Evaluation

| Evaluation Areas/Issues | Evaluators | Evaluation Methods |
|---|------------|---------------------|
| Effectiveness of teaching and assessment | Students | Direct and Indirect |
| Extent of achievement of course learning outcomes | Teachers | Direct |
| Quality of learning resources | Students | Indirect |

Evaluation areas (e.g., Effectiveness of teaching and assessment, Extent of achievement of course learning outcomes, Quality of learning resources, etc.)

Evaluators (Students, Faculty, Program Leaders, Peer Reviewer, Others (specify))

Assessment Methods (Direct, Indirect)

H. Specification Approval Data

| | |
|----------------------------|----------------------------------|
| Council / Committee | Program and study plan committee |
| Reference No. | |



| | |
|------|------------|
| Date | 25/08/2021 |
|------|------------|

